

Some division situations will produce a remainder, but the remainder should always be less than the divisor. If the remainder is greater than the divisor, that means at least one more can be given to each group (fair sharing) or at least one more group of the given size (the dividend) may be created. When using division to solve word problems, how the remainder is interpreted depends on the problem.

How does a remainder affect the answer in a division word problem?

Interpret a multiplication equation as a comparison, e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.

4.OA.A.2 - Use the four operations with whole numbers to solve problems ~ Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.1

4.OA.A.3 - Use the four operations with whole numbers to solve problems ~ Solve multistep word problems posed with whole numbers and having wholenumber answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

4.OA.B.4 - Gain familiarity with factors and multiples ~ Find all factor pairs for a whole number in the range 1-100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1-100 is a multiple of a given onedigit number. Determine whether a given whole number in the range 1-100 is prime or composite. operations, and/or the relationship between multiplication and division. (4.NBT.5) (4.NBT.6)

Translate comparative situations into drawings and equations with a symbol for the unknown and unknowns in all 3 locations. (4.OA.2)

Solve word problems involving multiplicative comparison using drawings and equations with a symbol for the unknown number and unknowns in all 3 locations. (4.OA.2)

Explain the difference between additive comparison and multiplicative comparison using visuals and words. (4.OA.2)

Read and write whole numbers up to a million using standard, word, and expanded form. (4.NBT.2)

Compare two multi-digit (up to a million) numbers. (4.NBT.2)

🔂 Use

manipulatives, pictures, and language to show the relationship between the numerals and their place value representations in multiple ways. (4.NBT.2)

Identify all factor pairs for any given number 1-100. Recognize that a whole number is a multiple of each of its factors. (4.OA.4)

Determine whether a given whole number in the range 1-100 is a multiple of

a given onedigit number. (4.OA.4)

Determine whether a given whole number in the range 1-100 is prime or composite. (4.OA.4)

Use visuals, symbols and/or language to explain their reasoning. (4.OA.4)

Multiply up to 4digit by 1-digit numbers and 2-digit by 2-digit numbers. (4.NBT.5)

Use place value manipulatives to represent multiplication calculations. Illustrate and explain the calculation by using written equations, rectangular arrays, and area models. (4.NBT.5)

Find wholenumber quotients and remainders with up to four-digit dividends and one-digit divisors. Illustrate and explain the calculation by using written equations, rectangular arrays, and area models. (4.NBT.6)

Use place value manipulatives to represent division calculations. (4.NBT.6)

Use the relationship between multiplication and division to explain calculations. (4.NBT.6)

Solve multistep word problems posed with whole numbers and having wholenumber answers using the four operations and represent those problems using equations with a variable standing for the unknown quantity.

| | | | | Interpret remainders when solving multi- step word problems (4.OA.3) Assess the reasonableness of answers using mental computation and estimation strategies, including rounding. (4.OA.3) | |
|----------|--|--|--|---|--|
| October | Enduring Understandings | Essential X Questions | Standards 8 | Knowledge & Skills | Academic Language |
| nber | 📅 Grade 4 Math Fract | ions: Equivalence | & Operations 7-8 weeks | | |
| November | Enduring Understandings | Essential X Questions | Standards 🔀 | Knowledge & 💥 Skills | Academic Language |
| | Fractions can be represented visually and in written form. Comparisons are valid only when the two fractions refer to the same whole. Fractions and Mixed Numbers are composed of unit fractions and can be decomposed as a sum of unit fractions. Improper Fractions and Mixed Numbers represent the same value. Addition and subtraction of fractions involves joining and separating parts referring to the same whole A product of a fraction times a whole number can be written as a multiple of a unit fraction. When converting measurements within one system, the size, length, mass, volume of the object remains the same. | How are fractions used in problem-solving situations? How are fractions composed, decomposed, decomposed, decomposed, decomposed, decomposed, compared and represented? Why is it important to identify, label, and compare fractions as representations of equal parts of a whole or of a set? How can multiplying a whole number by a fraction be displayed as repeated addition (as a multiple of a unit fraction)? Why does the size, length, mass, volume of an object remain the same when converted to another unit of measurement? | 4.NF.A.1 - Extend understanding of fraction equivalence and ordering ~ Explain why a fraction a/b is equivalent to a fraction (n × a)/(n × b) by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions. 4.NF.A.2 - Extend understanding of fraction equivalence and ordering ~ Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as 1/2. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model. 4.NF.B.3 - Build fractions from unit fractions ~ Understand a fraction a/b with a > 1 as a sum of fractions 1/b. 4.NF.B.3 - Build fractions from unit fractions ~ Understand addition and subtraction of fractions as joining and separating parts referring to the same whole. 4.NF.B.3 - Build fractions from unit fractions ~ Understand addition and subtraction of fractions as joining and separating parts referring to the same whole. | A fraction a/b is equivalent to a fraction (n x a)/(n x b). (4.NF.1) Fractions with different denominators can be compared by using visual fraction models, benchmark fractions, finding common denominators, and finding common numerators. (4.NF.2) Addition and subtraction of fractions as joining and separating parts referring to the same whole using manipulatives, pictures, symbols, language, and real-life examples. (4.NF.3) Recognize and generate equivalent fractions (4.NF.1) Compare 2 fractions with different numerators and different numerators by representing the fractions with symbols, visual models and words and by comparing to a benchmark fraction using symbols, visual models and words and words. (4.NF.2) Identify if | TIER 2 Benchmark fractions Common denominators Improper fraction Mixed numbers Visual fraction model Range TIER 3 Unit fractions Decompose Compose Equivalent Numerator Denominator Symbols Number line Line plot Distances (inches and feet) Intervals (of time) Elapsed time (seconds, minutes, hours, days, etc.) Liquid volume (fluid ounce, cup, pint, quart, gallon) Weight (ounce, pound, ton) Quarters Halves |

recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model.

4.NF.B.3c - Build fractions from unit fractions ~ Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.

4.NF.B.3d - Build fractions from unit fractions ~ Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

4.NF.B.4a - Build fractions from unit fractions ~ Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$.

4.NF.B.4b - Build fractions from unit fractions ~ Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number.

4.NF.B.4c - Build fractions from unit fractions ~ Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem.

4.MD.A.1 - Solve problems involving measurement and conversion of measurements ~ Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a twocolumn table.

4.MD.A.2 - Solve problems involving measurement and conversion of measurements ~ Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.

4.MD.B.4 - Represent and interpret data ~ Make a line plot to display a

comparisons are valid or invalid and explain why. (4.NF.2)

Represent unit fractions as a fraction with a numerator of 1 with manipulatives, pictures, symbols, language, and real-life examples. (4.NF.3)

Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. (4.NF.3)

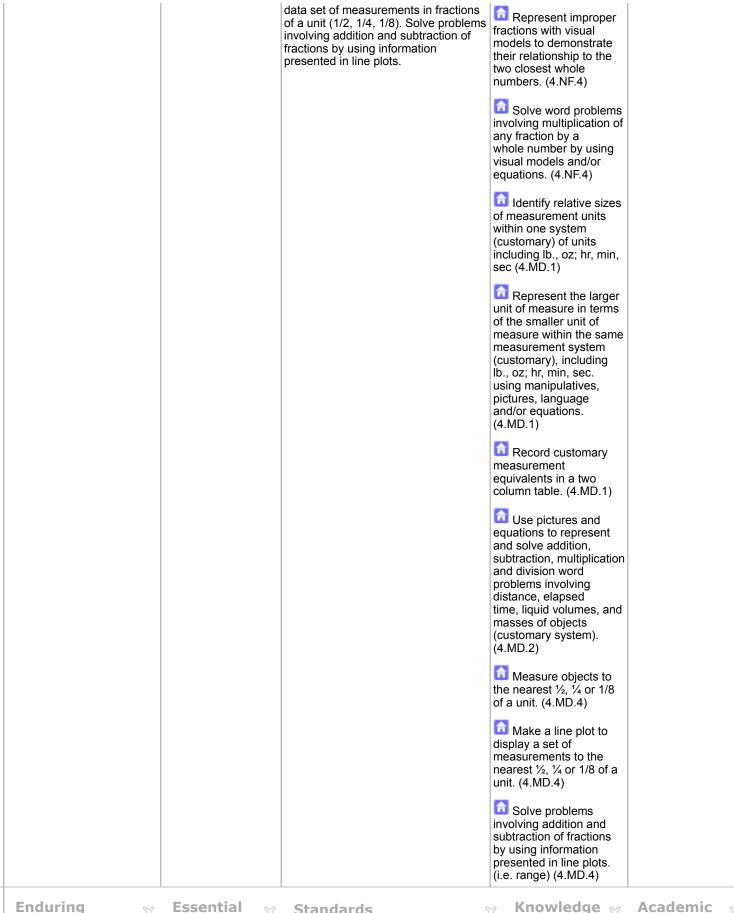
Add and Subtract mixed numbers with like denominators and model the decomposition of the mixed numbers into unit fractions using manipulatives, pictures, symbols, language, and real-life examples. (4.NF.3)

Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators using visual models and/or equations. (4.NF.3)

Represent multiplication of a fraction by a whole number as repeated addition using area or linear models. (4.NF.4)

Represent that a fraction, such as $\frac{3}{4}$, is made up of 3 unit fractions of $\frac{1}{4}$ using a multiplication equation, such as 3 x $\frac{1}{4}$ = $\frac{3}{4}$ (4.NF.4).

Multiply a fraction by a whole number by decomposing the fraction into a multiple of a unit fraction such as $\frac{3}{4} \times 2 =$ $3 \times 2 \times \frac{1}{4}$ which equals 6/4, using manipulatives, pictures, symbols, language, and real-life examples. (4.NF.4)



Essential Standards

Knowledge 👷 Academic 👷

| ember | Understandings | Questions | | & Skills | Language |
|------------------|----------------|-----------|-----------|---|----------|
| January December | Understandings | | Standards | Knowledge & Skills A fraction with a denominator of 10 can also be expressed as an equivalent fraction with a denominator of 100. A number can be represented as both a fraction and a decimal. Decimal comparisons are only valid when the two decimals refer to the same whole. Represent a fraction with denominator 10 as an equivalent fraction with denominator 100. (4.NF.5) Add two fractions with denominators 10 and 100 using manipulatives, pictures, written symbols, and language to explain the | Language |
| | | | | | |
| | | | | decimals to the hundredths using <, >, =. (4.NF.7) Identify if decimal comparisons are valid or invalid and explain why. (4.NF.7) | |
| | | | | Justify the conclusions using manipulatives, pictures, and/or language. (4.NF.7) | |

ebruary

Academic

Language

TIFR 2

Rules

Variable

Formula

TIER 3

Rounding

Estimation

Distance

Perimeter

Mass

Area

Metric units of

measurement

Liquid volume

Number patterns

Shape patterns

Grade 4 Math Computation Applications 5-6 weeks Knowledge & 💥 Enduring Essential Understandings X **Standards Ouestions** Skills 4.MD.A.1 - Solve problems involving Patterns are generated Datterns are Dia What strategies measurement and conversion of by following a specific rule. generated by following a can be used to find measurements ~ Know relative sizes specific rule. (4.OA.5) rules for patterns and of measurement units within one what predictions can Contraction and the second sec system of units including km, m, cm; the pattern support? Rounding can be be used when estimating kg, g; lb, oz.; l, ml; hr, min, sec. Within answers to real-world used to estimate a single system of measurement, Difference and the Hour International How are the four problems. reasonable answers express measurements in a larger unit basic operations for word problems. in terms of a smaller unit. Record The four operations are related to one (4.NBT.3) measurement equivalents in a twoanother? interconnected. column table. 1 How the four 🛅 How does 4.MD.A.2 - Solve problems involving 🛅 The standard algorithm operations can be used understanding place measurement and conversion of to solve real-world for addition and subtraction measurements ~ Use the four value help you solve and mathematical relies on adding or operations to solve word problems multi-digit addition problems. (4.OA.3) subtracting like base-ten involving distances, intervals of time, and subtraction units problems and how liquid volumes, masses of objects, and 🛅 The relative size of money, including problems involving can rounding be used measurement units Converting from larger to to estimate answers simple fractions or decimals, and within the metric system. smaller units of problems that require expressing to problems? (4.MD.1) measurement in the metric measurements given in a larger unit in system is done by terms of a smaller unit. Represent 🛅 How are the units multiplying by powers of ten 🔯 The formula for measurement quantities using of measure within the perimeter of geometric diagrams such as number line metric system figures. (4.MD.3) Derimeter is a real life diagrams that feature a measurement related? application of addition and scale. 🔟 The formula for area subtraction. 🔟 How do you find 4.MD.A.3 - Solve problems involving of rectangles. (4.MD.3) the area and measurement and conversion of 🔯 Area is a real life perimeter of measurements ~ Apply the area and Generate a pattern application of multiplication geometric figures and perimeter formulas for rectangles in and division. that follows a rule. how can using the real world and mathematical problems. (4.OA.5) formulas for perimeter and area help you 4.NBT.A.3 - Generalize place value <u>ם</u> Given a pattern, solve understanding for multi-digit whole identify the rule and realworld problems? numbers ~ Use place value extend the pattern and understanding to round multi-digit also identify apparent whole numbers to any place. features of a pattern that follows a given rule. 4.NBT.B.4 - Use place value which are not explicit understanding and properties of in the rule itself. (4.OA.5) operations to perform multi-digit arithmetic ~ Fluently add and subtract multi-digit whole numbers using the 🔯 Round multi-digit standard algorithm. whole numbers to a given place. (4.NBT.3) 4.OA.A.3 - Use the four operations

with whole numbers to solve problems

posed with whole numbers and having

whole-number answers using the four

equations with a letter standing for the

~ Solve multistep word problems

operations, including problems in which remainders must be interpreted.

Represent these problems using

reasonableness of answers using mental computation and estimation

4.OA.C.5 - Generate and analyze

patterns ~ Generate a number or

Identify apparent features of the

shape pattern that follows a given rule.

unknown quantity. Assess the

strategies including rounding.

Discrete Explain the rounding process using visuals and/or language. (4.NBT.3)

Add and subtract multi-digit whole numbers up to 1,000,000. (4.NBT.4)

Solve multistep word problems posed with whole numbers and having wholenumber answers using the four

| Fell | ormancePLUS | | | | 7/19/17, 2:40 | |
|-------|--|---|---|---|--------------------------------------|----|
| | | | pattern that were not explicit in the rule itself. | operations. (4.OA.3) | | |
| | | | | Represent multi-step word problems using equations with a variable standing for the unknown quantity. (4.OA.3) | | |
| | | | | Assess the reasonableness of answers using mental computation and estimation strategies, including rounding. (4.OA.3) | | |
| | | | | Represent the larger unit of measure in terms of the smaller unit of measure within the metric system, using manipulatives, pictures, language and/or equations. (4.MD.1) | | |
| | | | | Record measurement equivalents in a two- column table. (4.MD.1) | | |
| | | | | Use pictures and equations to represent and solve addition, subtraction, multiplication and division word problems involving measurement, distance, liquid volumes and masses of objects. (4.MD.2) | | |
| | | | | Solve problems involving area and perimeter of rectangles using visuals and equations that represent the formulas for area and perimeter of rectangles. (4.MD.3) | | |
| March | Enduring Understandings ^{XX} | Essential X Questions | Standards 8 | <pre>Knowledge & Skills</pre> | Academic Language | × |
| April | 🚮 Grade 4 Math 2-Dime | nsional Geometry | y 2-4 weeks | | | |
| A | Enduring Understandings | Essential Questions | Standards 8 | Knowledge 🕺 & Skills | Academic Language | ∝. |
| | by properties of their lines ty | What are the ypes of angles and he relationships? | 4.G.A.1 - Draw and identify lines and angles, and classify shapes by propertie of their lines and angles ~ Draw points, lines, line segments, rays, angles (right, | es segments, rays, right angles, acute angles, | TIER 2 Points | |
| | Angles are measured in | How are angles | acute, obtuse), and perpendicular and parallel lines. Identify these in two- | perpendicular lines, | End points Lines Line segments | |

| | | | | D |
|--|-------------------------------------|--|--|-------------------------------|
| the context of a central angle of a circle. | applied in the context of a circle? | dimensional figures. | identified within 2- dimensional figures. | Rays Angles (right, acute, |
| or a circle. | | 4.G.A.2 - Draw and identify lines and | (4.G.1) | obtuse) |
| Angles are composed of | 🖸 How are parallel | angles, and classify shapes by properties | | Central |
| smaller angles | lines and | of their lines and angles ~ Classify two- | Angles are formed | Adjacent angles |
| | perpendicular lines | dimensional figures based on the | wherever two rays | Perpendicular lines |
| | used in classifying | presence or absence of parallel or perpendicular lines, or the presence or | share a | Parallel lines |
| | two-dimensional | absence of angles of a specified size. | common endpoint. | Protractor Degrees |
| | shapes? | Recognize right triangles as a category, | (4.MD.5) | Symmetry |
| | 🔂 How are | and identify right triangles. | 🔂 An angle measure | Right triangle |
| | protractors used to | 4.G.A.3 - Draw and identify lines and | is a fraction of circular | Scalene triangle |
| | measure and aid in | angles, and classify shapes by properties | arc between | Isosceles triangle |
| | drawing angles and | of their lines and angles ~ Recognize a | the points where the | TIER 3 |
| | triangles? | line of symmetry for a two-dimensional | two rays intersect the | IIER 3 |
| | | figure as a line across the figure such | circle. (4.MD.5) | Plane (two- |
| | How can an | that the figure can be folded along the | | dimensional) figures |
| | equation be used to | line into matching parts. Identify line- symmetric figures and draw lines of | Benchmark angles and transfer their | Quadrilaterals |
| | solve a missing angle | | understanding that | Square |
| | measure when the | | a 360 degree rotation | Rhombus |
| | whole angle has been | 4.MD.C.5 - Geometric measurement: | about a point makes a | Rectangle Circle |
| | divided into two | understand concepts of angle and | complete circle | Triangle |
| | angles and only one | measure angles ~ Recognize angles as geometric shapes that are formed | to recognize and | Additive |
| | measurement is given? | wherever two rays share a common | sketch angles that measure | |
| | given. | endpoint, and understand concepts of | approximately 90 | |
| | | angle measurement | degree and 180 | |
| | | 4.MD.C.6 - Geometric measurement: | degree. (4.MD.5) | |
| | | understand concepts of angle and | | |
| | | measure angles ~ Measure angles in | An angle that turns | |
| | | whole-number degrees using a | through 1/360 of a circle is called a "one- | |
| | | protractor. Sketch angles of specified | degree angle," and | |
| | | measure. | can be used to | |
| | | 4.MD.C.7 - Geometric measurement: | measure | |
| | | understand concepts of angle and | angles. (4.MD.5) | |
| | | measure angles ~ Recognize angle | — | |
| | | measure as additive. When an angle is | Angle measure is | |
| | | decomposed into non-overlapping parts, the angle measure of the whole is the | additive (4.MD.7) | |
| | | sum of the angle measures of the parts. | A line of symmetry | |
| | | Solve addition and subtraction problems | for a two-dimensional | |
| | | to find unknown angles on a diagram in | figure is a line across | |
| | | real world and mathematical problems, | the figure such that | |
| | | e.g., by using an equation with a symbol for the unknown angle measure. | the figure can be | |
| | | _ | folded along the line into matching parts. | |
| | | 4.MD.C.5a - Geometric measurement: | (4.G.3) | |
| | | understand concepts of angle and measure angles ~ An angle is measured | | |
| | | with reference to a circle with its center at | 🛅 Draw points, lines, | |
| | | the common endpoint of the rays, by | line segments, rays, | |
| | | considering the fraction of the circular arc | right angles, acute | |
| | | between the points where the two rays | angles, obtuse angles, perpendicular lines, | |
| | | intersect the circle. An angle that turns | and parallel lines. | |
| | | through 1/360 of a circle is called a "one- degree angle," and can be used to | (4.G.1) | |
| | | measure angles. | | |
| | | _ | 🔂 Classify 2- | |
| | | 4.MD.C.5b - Geometric measurement: | dimensional figures | |
| | | understand concepts of angle and measure angles ~ An angle that turns | based on the | |
| | | through n one-degree angles is said to | presence or absence of parallel | |
| | | have an angle measure of n degrees. | or perpendicular lines | |
| | | | and right, acute or | |
| | | | obtuse angles. (4.G.2) | |
| | | | A. M. A. | |
| | | | ldentify and | |
| | | | classify triangles. | |

| | | | | Label the categories of triangles (right triangles, scalene, isosceles) (4.G.2) Recognize a line of symmetry for a two- dimensional figure as a fold-line, where the figure can be folded into matching parts. (4.G.3) Determine whether a figure has one or more lines of symmetry and draw lines of symmetry. (4.G.3) Identify the components of an angle and the number of degrees in a circle. (4.MD.5) I Use visuals and language to show the relationship between the components of an angle to a circle. (i.e. the center of the circle is the endpoint of the rays of the angle) (4.MD.5) Measure angles in whole-number degrees using a protractor. (4.MD.6) Sketch angles of a specified measure. (4.MD.6) Solve addition and subtraction problems to find unknown angles on a diagram of adjacent angles. (non- overlapping angles) (4.MD.7) | | |
|------|----------------------------|--------------------------|-------------|--|----------------------|---|
| May | Enduring Understandings | Essential X Questions | Standards X | Knowledge 💥 & Skills | Academic Language | × |
| June | Enduring Understandings | Essential X Questions | Standards X | Knowledge & Skills | Academic Language | × |